

Molecular Computation

A DNA-Based Model for Solving Mathematical Problems

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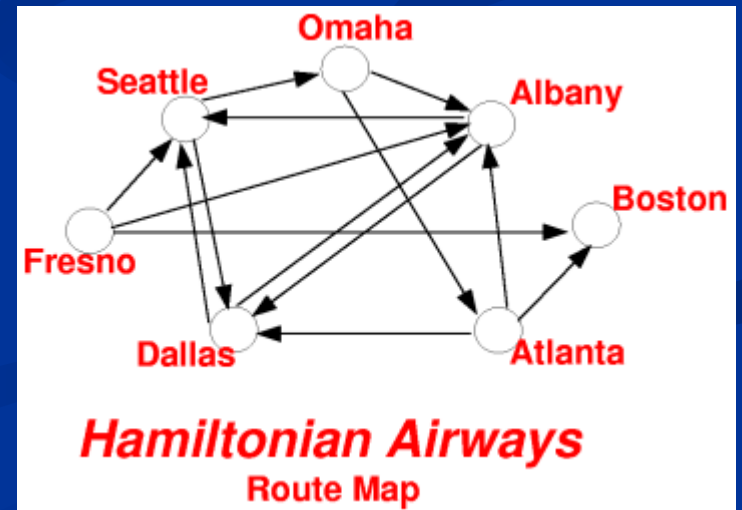
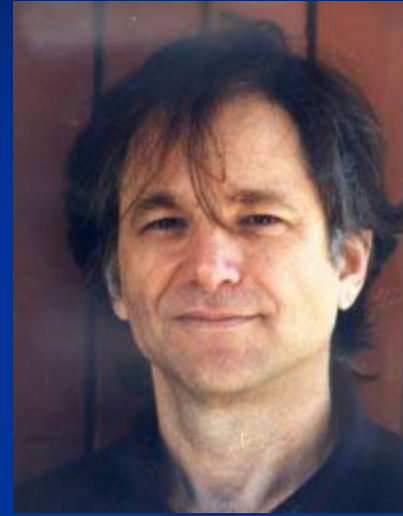
Dr. Anthony Macula

Topics

- What is DNA computing?
- What are the prerequisites for creating a DNA computing model?
- The two phases of the project
- Phase 1: Testing DNA strand binding
- The Geneseo problem
- Phase 2: Modeling the problem
- Future work

What is DNA Computing?

- An application of nanotechnology
- First developed in 1994 by Leonard Adleman
- Uses single stranded DNA molecules to represent the variables in a mathematical problem
- Selective hybridization then allows for the isolation of the correct answer



Why DNA?

- DNA has the ability to compute in *parallel*
- Standard computers compute in *series*
- This gives DNA the ability to sort through massive sets of data much quicker than a standard computer
- The key is simultaneous hybridization of DNA in solution

Example: Adding Numbers

5+3, 4+2, 3+6

Standard Computer:

$$5+3=8$$

$$4+2=6$$

$$3+6=9$$

Parallel:

$$5+3=8$$

$$4+2=6$$

$$3+6=9$$

Prerequisites

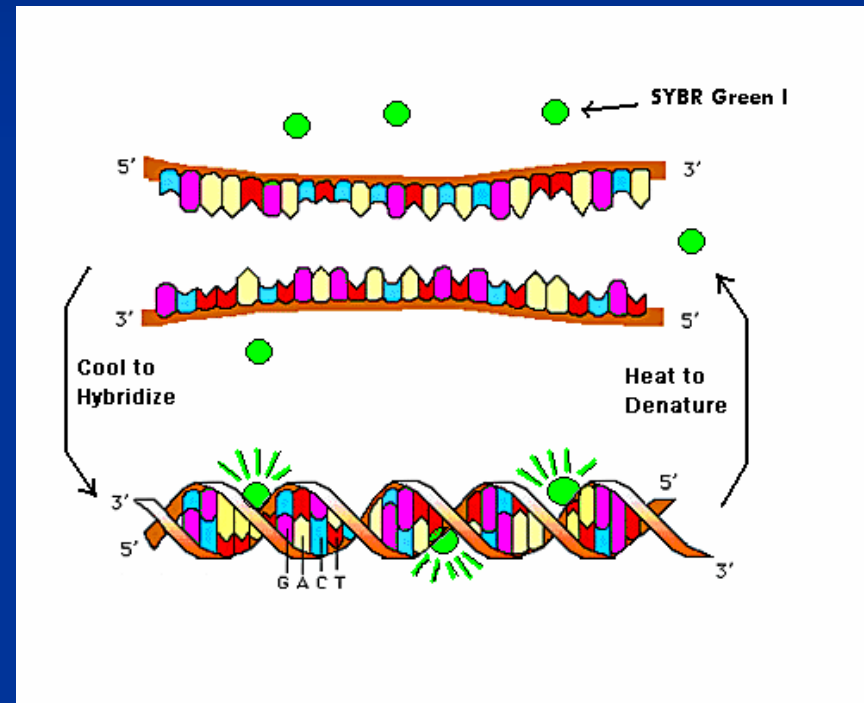
- Method for generating sequences of DNA to represent all the variables of a given problem
- Must also generate “well-behaved” strands
- Procedure for validating this method
- Strands that mis-pair when hybridizing will create errors in a DNA problem

Phase I

- Generated sequences using a computer algorithm developed by Dr. Anthony Macula
- Sequences were then synthetically prepared by *Invitrogen*
- Validated efficacy of the algorithm using SYBR Green I molecular dye
- This Dye binds to the minor groove of double stranded DNA (dsDNA) only

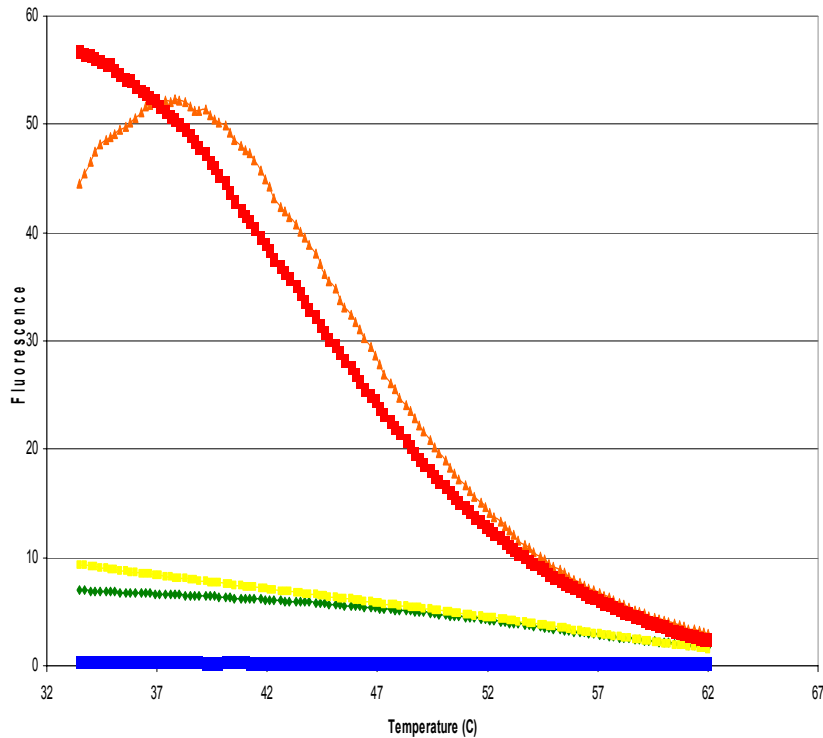
SYBR Green

- Place the generated strands in solution together
- Measure fluorescence to see if there is dsDNA present
- If there is notable fluorescence when it is not expected a DNA strand will be discarded and not used in the final experiment

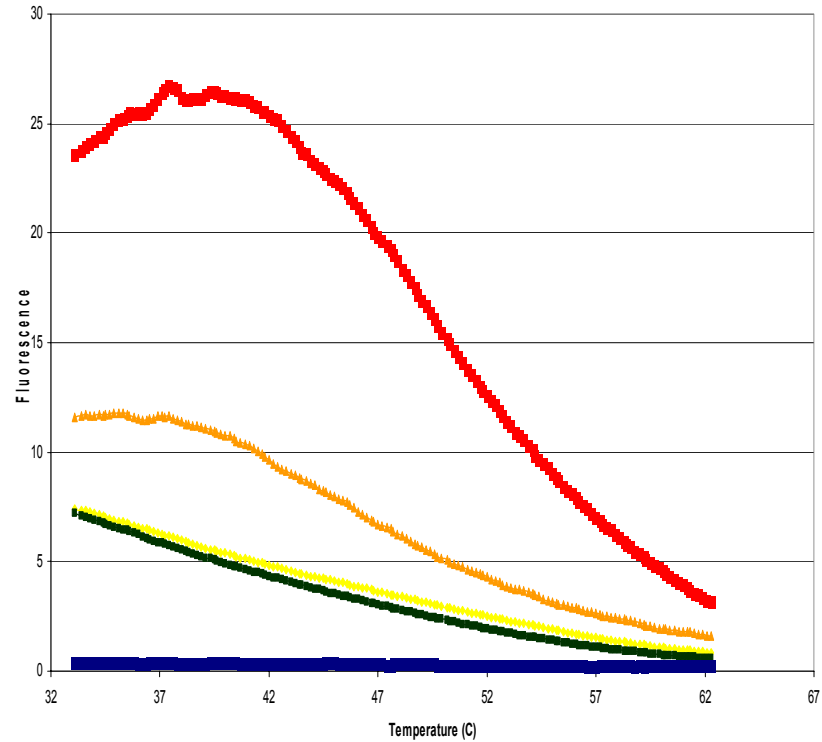


Fluorescence Experiments

Construct S14/C15

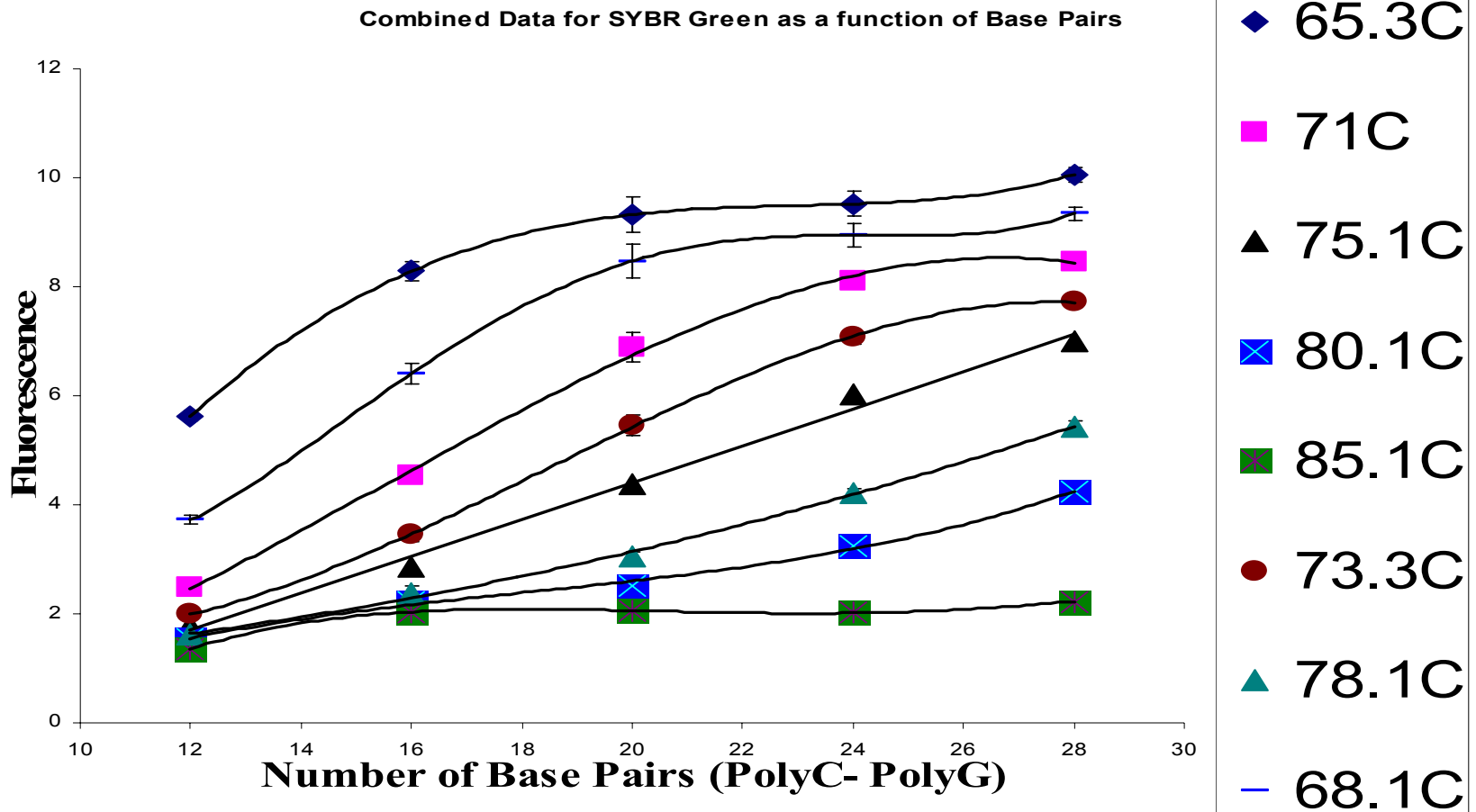


Construct S9/S10



Conclusion: SYBR Green was effective in screening for appropriate binding. The algorithm used to generate the sequences was efficient at producing “well-behaved” strands.

Other SYBR Experiments



The SAT Problem

- Short for *Satisfiability*
- A series of logic clauses connected by “and” statements
- Each clause must be true for the entire series to be true
- Each Variable is represented by two strands: One for TRUE and one for FALSE

In a SAT problem all clauses must be true!

Example:

- 1) X_1 or X_2
- 2) $\sim X_1$ or X_5
- 3) $\sim A_X$ or X_3 or X_4
- 4) X_3 or $\sim X_5$
- 5) X_4 or X_5
- 6) $\sim X_3$ or $\sim X_4$
- 7) $\sim X_2$ or X_3

It is easy to see that these problems can get incredibly complex as more clauses are added.

Answer: $A_1=T, A_2=T, A_3=T, A_4=F, A_5=T$

Phase II

Modeling the Problem

- The first step is to create all the possible answers to the problem
- The individual DNA strands must be linked together to produce all possible combinations
- Ex:

10 strands to code for **T** or **F** for **5** Variables

Each strand is **16 nucleotides** long there are

$2^5=32$ possible “solution” strands of length **80**

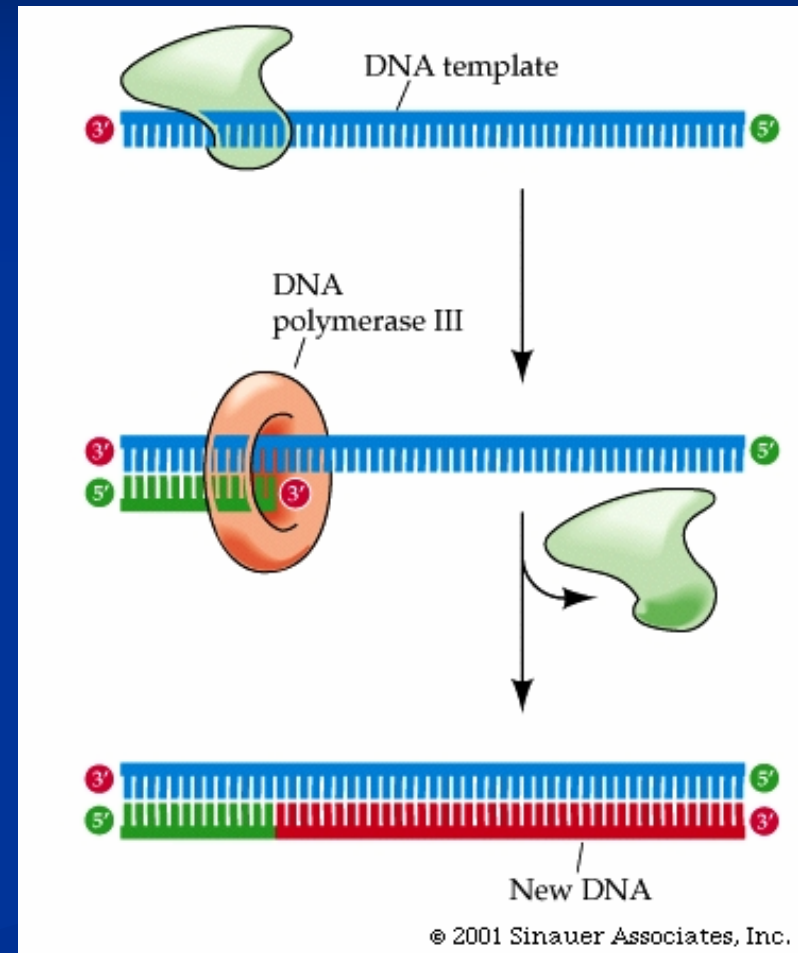
nucleotides (16 nucleotides * 5variables)

DNA Strands

- Library Sequences (5'—3')
- CCTTTTTTTTTTTTTTTT, T1
- TTCCAATTTCCTTAT, F1
- AACAAACCAAAACAAA, T2
- AAATCCTCTTTTCAAA, F2
- ACACACACTTTTACTT, T3
- ACTATCACAAAATAAA, F3
- CTTACTATTTCATTCAT, T4
- TAACCTACCTCTCCTT, F4
- CTATACCATCAATTAT, T5
- TAAATTCTCAACATTTA, F5

Building the Answers

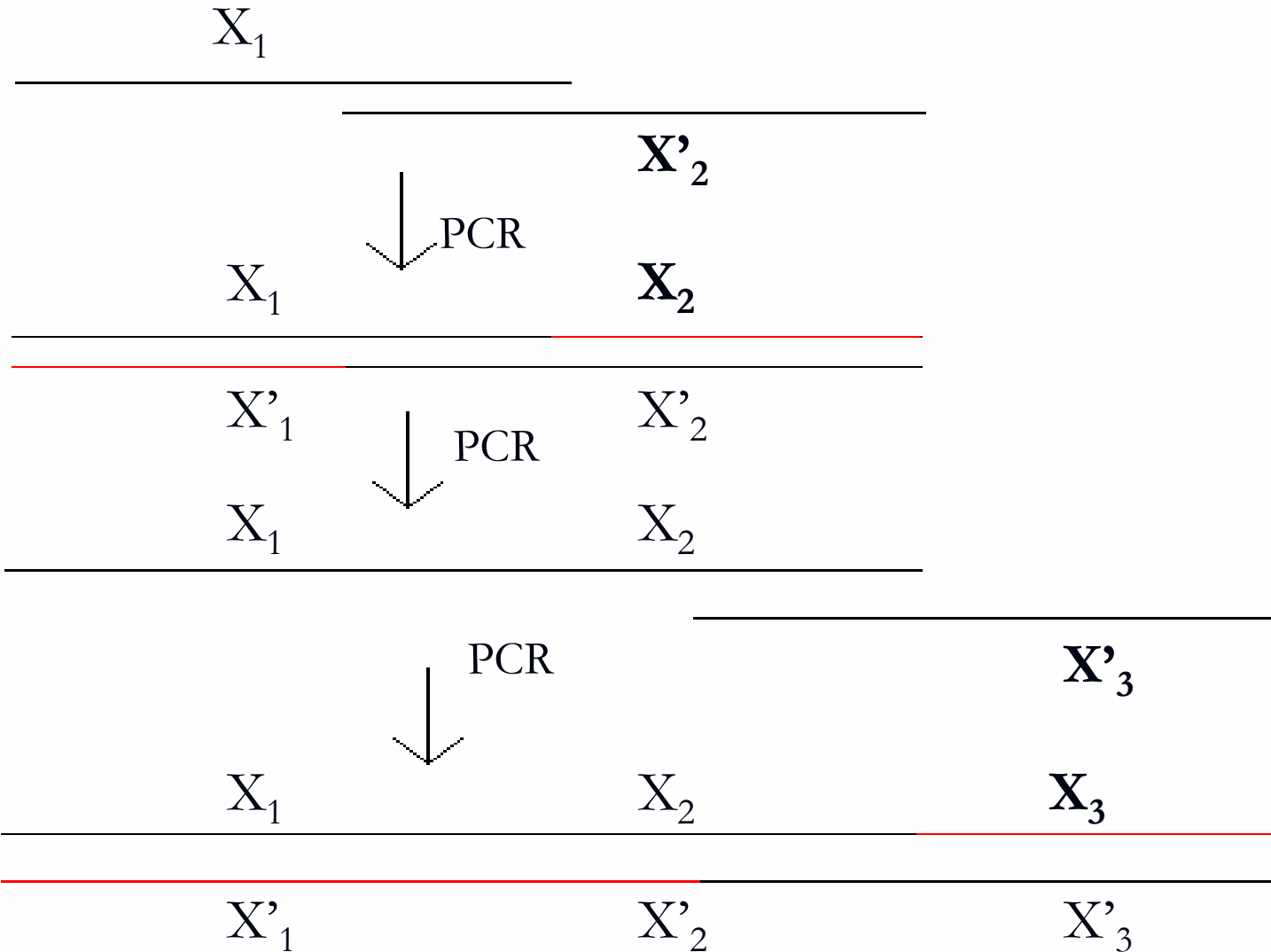
- DNA polymerase extends a DNA molecule by adding complementary bases to a primer
- We exploit this capability to create all combinations of the variable strands



Connecting the Pieces

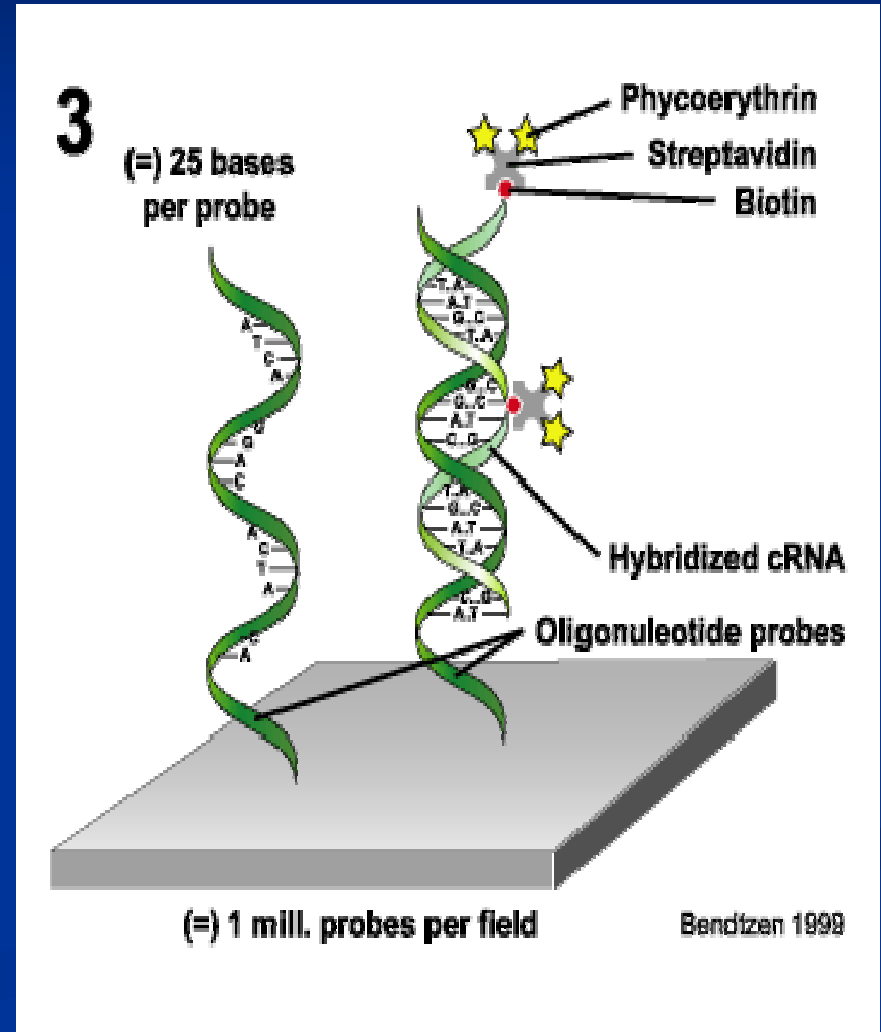
- Polymerase Chain Reaction (PCR): Repetitive heating and cooling of DNA sample to allow DNA polymerase to extend all the molecules
- Using complements to each new variable position all possible combinations of strands are created one PCR reaction at a time
- What is this slide talking about?

Stepwise PCR



Future Work

- The PCR reactions produce all 32 combinations, but it also creates their complements
- We need single-stranded DNA
- Use Biotin and Streptavidin to separate



Future Work

- Once all strands are single stranded the problem can be solved
- Bind complement sequences that make the first clause True to Streptavidin, which is also associated with metallic beads on a column
- Strands with the right combination will adhere to the column
- Pass the captured strands through successive columns representing TRUE for each clause in the problem
- Anything remaining at the end codes for the answer
- Sequence the strand

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